# Effects of Uniaxial Drawing and Heat-Treatment on Gas Sorption and Transport in PVC

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## Synopsis

Sorption and transport measurements for various gases in rigid poly(vinyl chloride) were made following uniaxial drawing and heat treatment. The permeabilities of He, Ar, N<sub>2</sub>, and CH<sub>4</sub> were found to be essentially independent of pressure in PVC while CO<sub>2</sub> showed a complex pressure dependence which varied with prior exposure and degassing history. Sorption isotherms were analyzed by the dual mode sorption model, and the parameters obtained were correlated with the Lennard–Jones potential-well depth of the gas. The Henry's law coefficient for CO<sub>2</sub> was found to be significantly larger than expected which is believed to be the result of a specific interaction with PVC. Uniaxial drawing of PVC above its glass transition caused significant reductions in gas permeabilities, of which roughly one-third is attributable to the accompanying heat treatment rather than molecular orientation per se. The physical state of the polymer was characterized by density, birefringence, and calorimetry. Changes in gas sorption and permeation behavior are discussed in terms of these results.

## INTRODUCTION

Fabrication and forming of polymeric products frequently involves a series of thermal and mechanical treatments which inevitably affect the final physical properties of the polymer. Apart from crystallinity, molecular orientation is one of the most important physical structural features of a polymer.

The effects of molecular orientation on gas transport in polymers often involve the simultaneous interplay of several variables, e.g., crystallinity, amorphous orientation, crystalline orientation, etc., which makes it difficult to assess each individual contribution separately. In the early studies on oriented semicrystalline polymers, changes in gas sorption and transport have routinely been interpreted in terms of changes in crystallinity and/ or crystalline orientation without concern about orientation in the amorphous phase.<sup>1-4</sup> However, over the past 15 years interest in amorphous orientation has grown steadily as indicated by the work of Brady and coworkers,<sup>5</sup> Barker et al.,<sup>6</sup> and most recently Porter and Wang.<sup>7</sup>

In view of the importance of orientation processes on transport behavior and the relatively sparse literature on the subject, we were prompted to initiate a series of studies in this area of which this first paper is devoted to poly(vinyl chloride). Our studies differ from most of the past work in several regards. First, it is recognized that gas permeation is the resultant of solubility and mobility phenomena, and either or both may be affected by orientation processes. Second, it is recognized that, to introduce molecular orientation in a polymer, the material is typically drawn above its

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glass transition temperature. Thus, the drawing process is almost invariably comprised of a thermal treatment in addition to molecular orientation. Therefore, in order to assess accurately the effects of orientation, the changes caused by the thermal treatment must also be determined. Most studies on molecular orientation to date have not devoted adequate attention to this issue. Also, knowledge of the extent of molecular orientation (such as draw ratio or an orientation function) alone is not sufficient for predicting the gas transport behavior of the material without knowledge of the *conditions* under which orientation was performed. The most important such processing variable is the drawing temperature. This study was designed while taking the above factors into account.

Only uniaxial orientation effects have been considered here. Biaxial orientation, having been partly examined, appears to affect gas transport in ways that differ fundamentally from those of the uniaxial case. Therefore, the results of this study must not be generalized to the biaxial case.

## **EXPERIMENTAL**

## Materials

Two PVC films were used in this study. The first was a 1.5 mil experimental film prepared by B. F. Goodrich which contained no additives except for 2% of a tin stabilizer.8 This film was used to characterize the gas sorption, transport and physical properties of rigid PVC and to serve as a reference material against which to check the other film used. The latter was a commercial product made by Klochner Pentaplast of America designated as Pentaform Type TH 170/01 which contained approximately 3 parts per hundred of an acrylic impact modifier. This film had excellent surface quality and thickness uniformity (nominally 5 mils) and was used for all oriented and annealed sample preparations. Table I lists some physical and mechanical properties for the two materials along with literature values.<sup>9</sup> Neither material showed any evidence by thermal analysis of an endotherm characteristic of ordinary primary crystallinity in the melting region known for semicrystalline PVC. However, a broad shallow curvature in DSC thermograms does appear above  $\sim 110^{\circ}$ C and is believed to be associated with the existence of roughly 5–10% imperfect crystalline order that is generally known to be present in commercial PVC.

The gases used for sorption and transport measurements were He, Ar, N<sub>2</sub>, CH<sub>4</sub>, and CO<sub>2</sub>. The purity of all gases was 99.7% or better except for CH<sub>4</sub>, which was 99.0%.

## **Sample Preparation**

A Table Model Instron fitted with an environmental chamber was used to prepare all the uniaxially drawn and annealed samples. The chamber was lined with insulation and contained heating elements, covered with aluminum foil to reduce radiation effects, and coupled to a power regulator and a temperature controller. Blowers were placed inside the chamber for internal circulation, and another, on the outside, provided forced air for

Film	Pentaform CS 5760 TH 170/01 Literature values®			
Source	B. F. Goodrich	Klockner Pentaplast	_	
Nominal thickness	1.5 mil	5 mil	_	
Glass transition	71°C	75°C	70-87°C	
Specific gravity	1.389	1.367	1.35 - 1.45	
Refractive index	1.544	1.539	1.52 - 1.55	
Yield (psi)	$7.99 imes10^3$	$8.08 imes10^3$	$5 extrm{-}9 imes10^3$	
Modulus (psi)	$3.05 imes10^5$	$2.68  imes 10^5$	$3.5-6 imes10^5$	
Percent elongation at break	107	135	2-40	

TABLE I Physical and Mechanical Properties for PVC Films Used

<sup>a</sup> From ref. 9.

rapid cooling of the samples once the drawing or annealing was completed. Temperature control and uniformity were within  $\pm 0.5$ °C.

Samples were prepared by first cutting  $4.5 \times 6$  in. rectangular strips of film along the original machine direction of the as-received film on which parallel lines 2 in. apart were drawn in ink along the transverse direction of the film. The film was then clamped at both ends by two pairs of wide T-shaped aluminum grips using small C-clamps. This assembly was mounted onto the crosshead mechanism of the Instron inside the chamber, which was heated beforehand to the desired drawing temperature. Transient reheating time to the drawing temperature was about 5 min. Following that, the sample was maintained at the working temperature for exactly 15 min. This was done whether the sample was drawn or just heat-treated. In the case of oriented samples, drawing was performed at the end of the heating period, e.g., 13 min heating followed by 2 min drawing. This procedure insured that samples of different draw ratios and the undrawn samples experienced an identical heat history so that the effects of orientation can be isolated from those of thermal treatment alone. Drawing at or above 75°C was done with a crosshead speed of 2 in./min (100% min), whereas, below 75°C, a slower strain rate of 0.5 in./min (25%/min) was required to prevent premature breakage of the films.

After drawing or annealing, each sample was air-quenched to room temperature by the external blower at a cooling rate of about 50°C/min. The draw ratio was determined by dividing the final distance between the ink lines by the initial distance of 2.0 in. In the case of drawing above  $T_g$ , deformation occurred uniformly throughout the sample and, thus, the nominal draw ratio defined above was also the actual draw ratio; for the sub- $T_g$  drawing, however, this apparent draw ratio was somewhat lower than the actual draw ratio because of the necking mechanism of deformation. The actual draw ratios were obtained by following additional ink lines drawn in the central region of the undrawn specimen. The reported draw ratios are actual and not nominal values.

Samples for sorption or permeation measurements were taken from the central section of oriented specimens to insure consistency in the comparisons of various samples and because only the central part of the drawn film satisfied the condition of truly uniaxial orientation.

## Sorption and Transport Measurement

The gas sorption measurements were carried out at 35°C using a dualvolume, dual-transducer cell design based on the pressure decay principle. Details about the components and operation of this device have been reported previously.<sup>10,11</sup> The only modification to the procedures described earlier is that in the case of N<sub>2</sub>, Ar, and CH<sub>4</sub> sorption, where solubility coefficients are very small, an increase in the sample volume from the usual 2 cm<sup>3</sup> to about double that amount brought about marked improvements in the acquisition and accuracy of the sorption isotherm data.

The equipment and procedures for the permeation measurements have also been described earlier.<sup>10,12</sup> The all-metal construction of the permeation cell allows gas transport measurements at pressures up to 30 atm. Time lag and permeability values were obtained by continuously monitoring the pressure rise downstream from the membrane. Very accurate thickness determinations for the samples were obtained by calculations based on the known membrane area, weight, and density and by a micrometer. Agreement between the two methods was excellent, and the thickness values used in calculations were always accurate to  $\pm 0.5 \ \mu m$ .

The permeability and time-lag measurements for Ar and N<sub>2</sub> on all the commercial Klockner films were done at a 20 atm upstream driving pressure. Since permeabilities for Ar and N<sub>2</sub> are of the order of  $10^{-12}$  and  $10^{-13}$  [cm<sup>3</sup>(STP) cm/cm<sup>2</sup> s cm Hg], it was necessary to achieve permeation rates high enough to render air leakage rates into the system insignificant. For He, a constant pressure of 3 atm was employed throughout. The level of accuracy and reproducibility for the transport data was within  $\pm 1.5\%$  of the reported values for P and about  $\pm 3\%$  for apparent diffusion and solubility coefficients. For sorption isotherms, a remarkable reproducibility of better than  $\pm 0.02$  cm<sup>3</sup>(STP)/cm<sup>3</sup> was obtained for N<sub>2</sub>, Ar, and CH<sub>4</sub> by doubling the sample size as indicated above. This was better than the precision level associated with the much more sorptive gas CO<sub>2</sub>.

## **Physical Characterization**

PVC density measurements were performed at 30°C in a density gradient column using aqueous solutions of calcium nitrate. Glass floats, factory-calibrated to  $\pm 0.0001$  g/cm<sup>3</sup>, were used to calibrate the liquid gradient. Density measurements were accurate within  $\pm 0.0002$  g/cm<sup>3</sup>.

Birefringence  $\Delta$  was used to characterize the state of orientation in uniaxially drawn PVC. The measurements were performed using a Babinet compensator with accuracy of  $\pm 0.05 \times 10^{-3}$ .

Thermal analysis of as-received, annealed and oriented PVC samples was performed on a Perkin-Elmer DSC-2 differential scanning calorimeter interfaced to a computerized control and data acquisition system. A scanning rate of 20°C/min was used in all cases. Sample weights were 15–18 mg, but all reported DSC results were normalized to a unit mass basis for comparison purposes.



Fig. 1. Sorption isotherms for N<sub>2</sub>, Ar, and CH<sub>4</sub> in PVC at 35°C.

#### GAS SORPTION AND TRANSPORT IN UNTREATED PVC

## Sorption

Figures 1 and 2 show sorption isotherms for  $N_2$ , Ar, CH<sub>4</sub>, and CO<sub>2</sub> at 35°C for the "as-received" B. F. Goodrich film. The solubilities for the Klockner sample did not differ significantly as Figure 21 shows for CO<sub>2</sub>. All of the isotherms are well described by the dual sorption model

$$C = k_D p + \frac{C'_H b p}{1 + b p} \tag{1}$$

Interpretations of the physical significance of the model and each of the parameters  $k_D$ ,  $C'_H$ , and b have been presented elsewhere.<sup>13,14</sup> Table II shows the sorption parameters for N<sub>2</sub>, Ar, CH<sub>4</sub>, and CO<sub>2</sub> at 35°C computed using a least-squares fitting algorithm. The sorption data and parameters presented here are the most extensive to be published for PVC to date. Berens<sup>15</sup> reported low-pressure sorption data for N<sub>2</sub> and CO<sub>2</sub> in PVC and estimated the dual mode parameters for the latter. Our  $k_D$  value for CO<sub>2</sub> agrees reasonably well with Berens' value of 0.7 cc(STP)/cc atm, but  $C'_H$  and b are substantially different, largely due to the narrow pressure range used in Berens' study, which precludes accurate estimates for these parameters.



Fig. 2. Sorption isotherm for  $CO_2$  in PVC at 35°C.

Gas	<i>ε/k</i> (K <sup>-1</sup> )	k <sub>D</sub> [cm <sup>3</sup> (STP)/cm <sup>3</sup> atm]	C' <sub>H</sub> [cm <sup>3</sup> (STP)/cm <sup>3</sup> ]	b (atm <sup>-1</sup> )	$k_D + C'_D b$	k <sub>a</sub>
N <sub>2</sub>	91.5	0.0169	0.4505	0.0448	0.0371	0.0341
Ar	124	0.0377	1.132	0.0410	0.0841	0.0800
CH₄	137	0.0513	2.305	0.0622	0.1946	0.2160
$CO_2$	190	0.587	8.939	0.2094	2.458	0.9644

TABLE II PVC Sorption Parameters for Various Gases at 35°C

The sorption extents for the various gases follow the ascending order of  $N_2 < Ar < CH_4 < CO_2$  as observed for all the other glassy polymers studied so far. The sorption data expressed in terms of the dual sorption model can be roughly correlated by plotting the logarithm of the sorption parameters against the Lennard–Jones potential parameter  $\epsilon/k$  for the gas,<sup>16</sup> as shown in Figures 3–6. The approximate linearity of the relationships has been established in previous studies.<sup>13,17–19</sup> In Figure 3 the straight line for log  $k_D$  vs.  $\epsilon/k$  was drawn using the N<sub>2</sub>, Ar, and CH<sub>4</sub> points only. The observed  $k_D$  value for CO<sub>2</sub> was about three times larger than the value expected based on the straight line correlation. This abnormally large CO<sub>2</sub> solubility may result from favorable polar interactions between the CO<sub>2</sub> and the PVC repeat unit, which are not present for the other gases. Similar, unexpectedly high CO<sub>2</sub> solubilities relative to other gases (e.g., CH<sub>4</sub>) have been reported recently by Koros<sup>20</sup> for cellulose acetate and PMMA. Those results have also been attributed to a specific gas/polymer interaction effect. In the



Fig. 3. Henry's law constant  $k_D$  vs. the Lennard-Jones parameter  $\epsilon/k$  (CO<sub>2</sub> point was not included in fitting the straight line).



Fig. 4. Hole saturation constant  $C'_H$  vs. the Lennard-Jones parameter  $\epsilon/k$ .

absence of specific gas/polymer interactions, plots of log  $k_D$  vs.  $\epsilon/k$  generally yield straight lines with essentially the same slope  $(0.96 \times 10^{-2} \text{ K}^{-1})$  for all polymers regardless of state (glassy or rubbery).<sup>17</sup> The slope of the line in Figure 3 is  $1.06 \times 10^{-2} \text{ K}^{-1}$  in reasonable agreement with other polymers and, thus, reinforces the notion that the CO<sub>2</sub> value is unusually large. A similar deviation from the linear line was not observed for CO<sub>2</sub> in the correlations involving  $C'_H$  and b, shown in Figures 4 and 5, respectively. This finding is important in that it further illustrates a fundamental distinction between the ordinary (Henry's law) and Langmuir gas dissolution modes.



Fig. 5. Hole affinity constant b vs. the Lennard-Jones parameter  $\epsilon/k$ .



Fig. 6. Apparent Henry's law coefficient measured by the equilibrium and transient methods vs.  $\epsilon/k$ : (()  $(k_p + C'_H)$  from sorption; (•)  $k_a$  from transport.  $p_2 \sim 1 - 2$  atm.

Figure 6 compares the initial slope of the sorption isotherm,  $k_D + C'_H b$ , with the apparent gas solubility coefficient,  $k_a$ , computed from transient permeation measurements at low driving pressures, i.e.,  $k_a = P/D_a$ , where the apparent diffusion coefficient is related to thickness and time lag by

$$D_a = l^2/6\theta \tag{2}$$

Based on the correlations seen in Figures 3–5, straight lines are not expected in Figure 6. The two measures of apparent solubility agree well (see Table II also) except in the case of  $CO_2$ .

#### Transport

Gas permeation in glassy polymers has frequently been analyzed using a dual mobility model,<sup>21</sup> which envisions the existence of two distinct diffusion coefficients,  $D_D$  and  $D_H$ , associated with the two modes of sorption. This model leads to the following expression for the permeability coefficient:

$$P = k_D D_D \left( 1 + \frac{FK}{1 + bp_2} \right) \tag{3}$$

where  $p_2$  is the upstream driving pressure,  $F = D_H/D_D$ , and  $K = C'_H b/k_D$ . In general, this expression suggests that P should be a mildly decreasing function of  $p_2$  as observed for a variety of glassy polymers.<sup>13,15-17</sup>

Permeability data for He, Ar,  $N_2$ , and  $CH_4$  in the B. F. Goodrich PVC are shown in Figure 7 as a function of upstream pressure. For the first three gases, there is no dependence of P on pressure implying the special case of



Fig. 7. Permeability of various gases in PVC at 35°C vs. the upstream driving pressure  $p_2$ .

"total immobilization" of the Langmuir mode or F = 0 in terms of the model embodied in Eq. (3). On the other hand, methane exhibits a small decline, about 5%, in P over this pressure range, but the  $CH_4$  data also exhibit more scatter than the data for the other three gases. In Table III, permeabilities and apparent diffusion coefficients for the various gases in the two PVCs are tabulated along with values extracted by interpolation from the data of Tikhomirov et al.,<sup>22</sup> which is the only extensive source in the literature reporting on the transport of various gases in unplasticized PVC. Our data agree quite well with the reported values for He and Ar, but diverge greatly for the other gases, particularly N<sub>2</sub> and CH<sub>4</sub>. Roberts and Kammermeyer<sup>23</sup> have also reported some results for He, CH<sub>4</sub>, and CO<sub>2</sub>, but their P values are another order of magnitude larger than Tikhomirov's values. Our results follow reasonable trends while the Tikhomirov data contain some inconsistencies. For example, this reference gives nearly identical permeabilities for Ar and N2 whereas, based on the behavior of other polymers, one expects N<sub>2</sub> to always have both a lower solubility and lower

P [cm<sup>3</sup>(STP)cm/cm<sup>2</sup> s cm Hg]  $D_a (\rm cm^2/s)$ CS5760 Gas Pentaform Tikhomirov Pentaform CS5760 Tikhomirov He  $3.36 \times 10^{-10}$  $2.98 \times 10^{-10}$  $3.1 \times 10^{-10}$  $4.0 \times 10^{-6}$ Ar  $3.69 \times 10^{-12}$  $2.77 \times 10^{-12}$  $2.7 imes10^{-12}$  $3.39 imes10^{-9}$  $2.42 \times 10^{-9}$  $2.3 \times 10^{-9}$  $N_2$  $9.45 \times 10^{-13}$  $6.68 \times 10^{-13}$  $2.8 \times 10^{-12}$  $1.88 \times 10^{-9}$  $1.37 \times 10^{-9}$  $8.0 imes 10^{-9}$ CH₄  $1.08 \times 10^{-12}$  $8.50 imes10^{-13}$  $6.0 imes 10^{-12}$  $3.31 \times 10^{-10}$  $3.1 \times 10^{-9}$  $2.43 \times 10^{-11}$  $CO_2$  $1.84 \times 10^{-11}$  $3.2 \times 10^{-11}$  $1.45 \times 10^{-9}$  $1.45 \times 10^{-9}$  $5.5 imes10^{-9}$ 

Permeability<sup>\*</sup> and Apparent Diffusion Coefficients of Various Gases in Two PVCs at 35°C along with Values Interpolated from the Data of Tikhomirov et al.<sup>22</sup>

<sup>a</sup> Upstream pressures for He, Ar, N<sub>2</sub>, and CH<sub>4</sub> measurements of *P* and  $D_a$  were 20 atm for the Pentaform film and 0.5-2.0 atm for the other two materials. For CO<sub>2</sub> an upstream pressure of ~1.0 atm was used for all three materials.

diffusion coefficient than Ar. The diffusion coefficient for  $CH_4$  given in the Tikhomirov paper is larger than that of Ar (see Table III), which is not physically realistic since the molecular diameter of  $CH_4$  is larger than that for Ar. The *P* and  $D_a$  values for the commercial Klockner product are somewhat larger than those for the B. F. Goodrich film due to the impact modifier and possibly to differences in the thermal histories of the two samples. Figure 8 shows time lag data for  $CH_4$ ,  $N_2$ , and Ar in the experimental PVC film as a function of upstream driving pressure. As expected,  $CH_4$  shows a stronger decrease in  $\theta$  with  $p_2$  than do  $N_2$  or Ar.

The permeation of  $CO_2$  in PVC is a complex function of prior history as demonstrated in Figure 9. The curve labeled "1" represents an initial sequence of runs made on as-received film by sequentially increasing the pressure from 1 atm to about 25 atm, allowing adequate time at each pressure to reach an apparent steady-state. For high pressure, this took much longer than the usual four to five time lags which proved sufficient for the other gases. For the 25 atm measurement, the pressure was held for 24 h, after which the film was degassed for 35 h or about 90 time lags. A second sequence of measurements were made on the same film again beginning at 1 atm and progressing sequentially to higher pressures. As seen in Figure 9, this gave significantly higher permeabilities, especially at low pressures, than did the first sequence. After this, the sample was removed from the permeation cell and then reinstalled after one week. After degassing for 24 h, the third sequence of measurements were made in the same manner as the first two. Finally, after the maximum pressure of 25 atm was reached, the pressure was varied randomly up and down the pressure scale without evacuation between runs, giving curve 4 in Figure 9. Each run lasted until no change in flux occurred over at least 10 h, and the so-obtained permeabilities are essentially independent of pressure as seen for the other gases. This complex behavior is a consequence of a rather significant plasticizing influence of  $CO_2$ , which alters the state of glassy polymers even after the  $CO_2$  is removed. Such "conditioning" effects have been observed before<sup>19,24,25</sup> for other glassy polymers; however, PVC appears



Fig. 8. Time lag vs. the upstream driving pressure  $p_2$ , for Ar, N<sub>2</sub>, and CH<sub>4</sub> in PVC at 35°C.



Fig. 9. Permeability of CO<sub>2</sub> in PVC at 35°C as a function of upstream driving pressure  $p_2$ . Runs were made in four sequences, in ascending pressure order: ( $\bigcirc$ ); 1st sequence; ( $\bigcirc$ ) 2nd sequence after 36 h evacuation; ( $\bigtriangledown$ ) 3rd sequence after 1 week evacuation; ( $\Box$ ) 4th sequence with no evacuation from 3rd sequence.

to be different in that the changes in state occur over longer time periods and may be less stable once established than those observed for other glassy polymers. The strong influence of  $CO_2$  on PVC is made clear by the observation that sorption of  $CO_2$  at 25 atm lowers the  $T_g$  by about 25°C as described elsewhere.<sup>26</sup> Owing to the severe time dependence of the  $CO_2$  conditioning on PVC permeation characteristics, care must be exercised in attempts to interpret the effect of pressure on permeability. For example, curves 1–3 in Figure 9 might be regarded to be in accord with various models which predict P to increase with  $p_2^{27,28}$  whereas, in fact, upon more complete conditioning the permeability appears to be independent of pressure (curve 4). In this case, transport behavior is not just a function of  $CO_2$  concentration or pressure, but also depends on long term relaxations at any given condition.

Time lag data for PVC in  $CO_2$  is plotted as a function of pressure in Figure 10. The conditions under which these values were measured were very strictly controlled to obtain the most reproducible data possible. A 2-mil film different from the one used for P determinations was initially "vec-



Fig. 10. Time lag data for  $CO_2$  in PVC as a function of upstream driving pressure  $p_2$  at 35°C. The sample was initially exposed to 20 atm  $CO_2$  for 3 days on the upstream side. Evacuation time between runs was ~10 h.

tored" (i.e., exposed to  $CO_2$  on the upstream side only) with 20 atm of  $CO_2$  for 3 days. Before each run, the sample was evacuated 12–15 h, and the runs were carried to between 5 and 7 time lags at each pressure. The pressure sequence used for the runs was based on random selection. Over the pressure range from 2 to 20 atm, the time lag decreased by 30%. The corresponding time lag reductions for  $CH_4$ ,  $N_2$ , and Ar were 16% for  $CH_4$  and 10% for  $N_2$  and Ar.

# EFFECTS OF ANNEALING AND ORIENTATION

The following describes the effects of various treatments on properties of PVC. As mentioned earlier, certain annealing or heat treatment effects accompany any response caused by the drawing operation. To isolate this effect from orientation, some samples were given the same heat treatment but were not drawn, and they are referred to as having a draw ratio  $\lambda$  of 1.0 or by the notation 1.0X. Orientation of PVC was easiest to achieve at temperatures not far removed from  $T_g$ . In the range of temperatures from above 50 to 115°C, drawing could be performed with relative ease to 3.0X with 2.8X being the limit at 50°C. Thus, at  $\lambda = 3.0$ , the effect of drawing temperature was investigated. The maximum draw ratio possible under our operating conditions (~4.2X) was attainable at 100°C. This temperature was selected for study of the widest possible range of draw ratios on PVC properties.

The gases used to investigate the transport responses of PVC to various treatments were He, Ar, and N<sub>2</sub>. Both CH<sub>4</sub> and CO<sub>2</sub> were excluded since CH<sub>4</sub> presented difficulty because of its very long time lags ( $\sim 20$  h for a 5 mil film) and CO<sub>2</sub> was avoided because of the complicated pressure and time dependence issues described earlier. For equilibrium sorption measurements, on the other hand, CO<sub>2</sub> is the only gas for which data are reported. It was difficult to discern differences in equilibrium sorption for Ar and N<sub>2</sub> since the changes induced were of the order of the accuracy limitations inherent in the sorption system so that apparent solubility behavior derived from transient permeation experiments was monitored instead.

## Birefringence

The birefringence  $\Delta$  of PVC drawn at 100°C is shown in Figure 11 as a function of draw ratio. The curve, characteristic of the pseudo-affine deformation mechanism,<sup>29</sup> is typical of many polymers drawn above  $T_g$ . The dependence of birefringence on the drawing temperature for fixed draw ratios is shown in Figure 12. The birefringence, and hence chain orientation, is markedly reduced as the drawing temperature is increased. A reduction of 65% is observed for a 2X-drawn sample over the temperature range from 55 to 125°C. The birefringence curves are continuous over the entire temperature range, i.e., no break at  $T_g$ , suggesting that the mechanism of chain alignment taking place both above and below  $T_g$  changes in a continuous manner. The birefringence plots of Figures 11 and 12 agree well with similar data for PVC from other sources, e.g., Hibi et al.<sup>30</sup> and Robinson and Bower.<sup>31</sup>

Exposure of oriented PVC film to high  $CO_2$  pressures did not have a significant effect on the orientation state as Figure 13 illustrates for a



Fig. 11. Birefringence versus draw ratio for PVC drawn at 100°C.



Fig. 12. Dependence of PVC birefringence on the drawing temperature at constant draw ratios of 2.0 and 3.0.



Fig. 13. Effect of  $CO_2$  exposure at 35°C on the birefringence of oriented PVC ( $\lambda = 4.1$ ). Exposure duration was 24 h at each pressure.



Fig. 14. Dependence of density for annealed ( $\lambda=1.0)$  and drawn ( $\lambda=3.0)$  PVC on the processing temperature.

sample drawn to 4.1X. The point at zero pressure represents the birefringence of the original sample before any exposure to  $CO_2$ . This sample was exposed to  $CO_2$  at 35°C at successively higher pressures for 24 h each, and the birefringence was measured subsequent to every exposure. The approximate 5% drop in birefringence noted in Figure 13 may be due mainly to post-drawing relaxation at 35°C rather than to  $CO_2$  exposure since  $CO_2$ exposure is expected to be more effective at high pressures and not at pressures up to 10 atm where the decrease occurs.

## Density

The effect of annealing and drawing on PVC density is shown in Figure 14 for a wide range of treatment temperatures. Heat treatment above  $T_g$  was predominantly responsible for all important density changes in PVC. Density increased with increasing annealing temperature and leveled off to an essentially constant value for temperatures  $\geq 110^{\circ}$ C. The "as-received" Klockner PVC is a calendered product that most probably had been quenched from high processing temperatures which explains its low density compared to heat-treated and drawn samples. It is not clear, however, why the density dips below the "as-received" value for the sample annealed at 70°C (below  $T_g$ ). This reduction in density is also accompanied by an increase in argon diffusion coefficient as shown later.

The shape of the  $\lambda = 3.0$  curve relative to that of  $\lambda = 1.0$  is interesting. At drawing temperatures below  $T_g$  (up to 82°C) the density increases slightly relative to the "as-received" value as a result of drawing, while above 82°C drawing yielded lower density films compared to samples with the same thermal treatment but not drawn. Densification due to post-yield drawing below  $T_g$  has also been observed for polycarbonate.<sup>32,33</sup> Values of P and  $D_a$ are consistent with the observed increase in density with sub- $T_g$  drawing. The air quenching procedure was applied uniformly to all the samples, but since the drawn samples were thinner than the annealed ones, they cooled somewhat faster. This may partly explain the slightly lower densities for the oriented samples in Figures 14 and 15. In Figure 15, the density of PVC is plotted as a function of draw ratio for a drawing temperature of 100°C.



Fig. 15. PVC density as a function of draw ratio: ( $\bigcirc$ ) drawn at 100°C; ( $\bigcirc$ ) drawn at 100°C, then annealed (15 min).

The upper curve is for samples which were annealed under stress immediately following drawing. This annealing treatment was found to cause a slightly larger density at high draw ratios compared to samples which were simply drawn—see lower curve. It is apparent, therefore, that annealing above  $T_g$  and not orientation per se is mainly responsible for the densification of PVC.

The density results presented here cannot be compared directly with those reported by Brady et al.<sup>5</sup> since they did not make clear the effects that heat treatment had on the density. The results of the following calorimetric study give a clearer insight into the nature of physical changes occurring in PVC as a result of annealing and orientation.

## **Differential Scanning Calorimetry**

The purpose of the calorimetric study was to determine whether the PVC samples used in this study were crystalline or not and to monitor any important physical changes occurring in the polymer due to the various processing steps. The scanning range for the thermograms reported here is from 17 to 227°C. The PVC melting point, estimated from Reding et al.'s study,<sup>34</sup> should be about 192°C for the material used in this work. For accurate comparison between the various DSC scans, all the thermograms were normalized to a 1 mg basis and accurate subtractions between endotherms were performed digitally by the computerized Thermal Analysis Data Station. All thermograms considered here are "first heats" following every particular treatment. DSC heats following the first were not of interest since the effects of sample history are erased during the course of the first heat; and, in fact, second heats looked essentially identical for all samples.

The effects of annealing at various temperatures above  $T_g$  ranging from 78 to 135°C are shown in the series of DSC scans presented in Figure 16 arranged in ascending order according to annealing temperature. The following features characterize the scans of Figure 16: (a) no melting endotherm near 192°C is associated with any of the annealed samples; (b) an



Fig. 16. DSC scans for samples annealed at various temperatures above  $T_{g}$ .

endothermic peak occurs near  $T_g$  which is about 75°C; (c) another endothermic peak occurs above  $T_{\epsilon}$  and shifts to higher temperatures as the annealing temperature is increased; and (d) a small endothermic "hump" of fixed size and position (135°C) also appears for all samples. The peak near  $T_{g}$ , which does not appear for all samples, is the result of different time spans between the sample preparation and DSC testing for different samples, i.e., room-temperature annealing. Not all the samples were prepared at the same time, and those samples which were exposed to ambient conditions for long periods developed the observed sub- $T_g$  peak. Since the samples annealed at 85, 125, and 135°C were prepared only several hours prior to DSC testing they do not show any trace of such a peak. The second peak above  $T_g$  is a more interesting feature of the thermograms. This peak varies in both area and position as a function of the annealing temperature, and thus appears as a characteristic feature of annealing above T. The peak's position was always found to be  $10-15^{\circ}$ C above the annealing temperature, as shown in Figure 17. Such endothermic behavior for annealed PVC agrees well with the findings of several studies.<sup>5,35-37</sup> These peaks are suggestive of molecular order which is introduced into the polymer by annealing above  $T_{e}$ . This order is currently referred to in different ways. It is denoted by "secondary crystallinity," "mesomorphic order," or simply "molecular order." It is agreed upon among the various authors, however, that such regions possess a substantially lower degree of order than does conventional primary crystallinity. The order can be viewed to be arising from close packing of short chain segments especially those containing long sequences of syndiotactic dyads. Annealing above  $T_{e}$  has also been reported to increase the ratio of trans/gauche rotational isomers,38 which would facilitate such an ordering process.

The area under the DSC annealing peak varies in an interesting manner. Since it was difficult to define the DSC endothermic area in an absolute manner, this area was defined by first subtracting the normalized DSC thermogram for the as-received sample from each of the annealed sample scans. The difference curve, which carried the annealing endotherm with it, was then analyzed. Figure 18 shows such a subtraction for a sample annealed at 115°C. The results of similar subtractions for annealing temperatures from 78 to 135°C are shown in Figure 19. The sub- $T_g$  region subtraction was suppressed in these curves since it is irrelevant and would



Fig. 17. DSC peak temperature for annealed PVC versus annealing temperature.



Fig. 18. DSC scans showing the effect of annealing at 115°C.

be confusing. Upon subtraction, a more subtle feature of these annealing endotherms appears in Figure 19 and that is the actual splitting of this endothermic region into two peaks, the first being fixed at 90°C whereas the second and smaller peak varies in position with annealing temperature as described earlier. The endothermic area was defined as the area between the DSC subtraction curve and the base line over the entire temperature range. This area was converted into cal/g to represent the "fusion" energy associated with the loss in order developed during annealing. It must be noted that only the second and smaller annealing peak changes in area and position with annealing temperature. Since this peak overlapped the 90°C peak at lower annealing temperatures and, thus, could not be separated from it, the entire area under the both peaks was analyzed. The calculated heats of fusion for the curves shown in Figure 19 are plotted against the annealing temperature in Figure 20. The dependence of  $\Delta H$  on annealing temperature is quite interesting, exhibiting an increase up to the region of 100–110°C, where  $\Delta H$  reaches a maximum and then begins to decline for



Fig. 19. DSC scans of PVC for various annealing temperatures after subtraction of "asreceived" scan. (Sub- $T_g$  events were suppressed from these curves for easier comparison.)



Fig. 20. Endotherm area versus annealing temperature for PVC.

higher annealing temperatures. This agrees well with the results of Brady et al.,<sup>5</sup> but differs from Brown et al.'s,<sup>37</sup> which places this maximum at 130°C. The shape of this curve is logical since ordering processes usually require an optimal segmental mobility or temperature that corresponds to the highest rate of ordering as in the case of crystallization.

Annealing PVC at temperatures below  $T_g$  did not induce any of the effects discussed above. Figure 21 shows how the net effect of sub- $T_g$  annealing was to merely shift to a higher temperature the sub- $T_g$  annealing peak, which is a very well-known phenomenon. The size and position of this peak are dependent on both annealing time and temperature. An extensive study on this topic has been done by Berens and Hodge.<sup>39</sup>

The effect of drawing PVC above the glass transition on the order introduced by annealing the polymer is quite unexpected. Figure 22 illustrates this effect by the subtraction of a 1.OX sample from a 4.2X sample subjected to the same heat treatment. The subtraction yields a substantially negative difference reflecting a strongly reduced order for the 4.2X sample relative to the undrawn but annealed sample. Evidently, the chain segments that form ordered bundles under annealing conditions are subjected to stress under drawing such that the bundle order is distorted. Furthermore, superimposed on this reduction in the annealing order is a lowering in the



Fig. 21. DSC scans showing the effect of annealing at 70°C (sub- $T_e$ ).



Fig. 22. DSC scans showing the effect of uniaxial drawing above  $T_{s}$ .

base line for the oriented sample in the region above  $T_g$ , suggesting a reduction in the heat capacity due to orientation. Orientation in amorphous polymers has been thought to cause reductions in the heat capacity and is known to reduce the thermal conductivity of the material.<sup>39-41</sup> The broad and shallow curvature that appears in the DSC baseline above ~110°C is probably indicative of some crystalline or mesomorphic order which is known for PVC, but this DSC curvature was almost identical for samples subjected to different annealing treatments as well as for the as-received film.

## CO<sub>2</sub> Sorption

Since gas transport through polymers is the resultant of both sorption and diffusion, independent examination of the two processes is necessary. The sorption isotherms for  $CO_2$  in PVC subjected to annealing and orientation at 85°C are shown in Figure 23 along with that of an "as-received" sample. Model parameters are given in Table IV. The extent of  $CO_2$  sorption



Fig. 23. CO<sub>2</sub> sorption isotherms at 35°C for PVC: ( $\bigcirc$ ) as received; ( $\bigcirc$ ) heated at 85°C (15 min); ( $\Box$ ) drawn to 3.0X at 85°C.

TABLE IV CO<sub>2</sub> Sorption Parameters at 35°C for PVC Subjected to Annealing and Orientation at 85°C

is reduced by the thermal treatment at 85°C and drawing to 3.OX in addition produces only a modest further reduction compared to the as-received material. Similar responses for Ar and  $N_2$  were seen in the apparent solubility coefficients deduced from transport measurements.

## Transport of He, Ar, and N<sub>2</sub>

Permeabilities for He, Ar, and N<sub>2</sub> are plotted against the draw ratio in Figure 24. The relative permeability  $P/P_0$  used to correlate the data is simply the ratio for a given gas of the permeability P for the treated material to the "as-received" permeability value  $P_0$ . Values for  $P_0$  are tabulated in Table III under the Pentaform heading. The drawing temperature for all these samples was 100°C as is the case for Figures 25-31. Note that the  $P/P_0$  curves do not go through  $P/P_0 = 1.0$  at  $\lambda = 1.0$ , reflecting the effect of heat treatment, which was the same for samples of all draw ratios. Figure 25 shows the same  $P/P_0$  results plotted against film birefringence. The birefringence is a more physically meaningful correlating parameter as it represents a quantitative measure of the actual extent of chain alignment in the polymer as opposed to the draw ratio which is a macroscopic quantity that usually does not describe the microscopic orientation state in the system. The chain orientation function f, which can be defined as the fraction



Fig. 24. Permeability, relative to "as-received" value  $P_0$  at 35°C for He, Ar, and N<sub>2</sub> in PVC as a function of draw ratio. (Drawing temperature = 100°C.)  $P_0$  values are tabulated in Table II.



Fig. 25. Relative permeability at 35°C for He, Ar, and  $N_2$  as a function of birefringence. (Drawing temperature = 100°C.)

of polymer segments aligned along the drawing axis, is related to bire-fringence  $\Delta$  by

$$f = \Delta/\Delta^0 \tag{4}$$

where  $\Delta^0$  is the intrinsic birefringence or the limiting  $\Delta$  value for the completely oriented material. The intrinsic birefringence can be evaluated theoretically using the polarizabilities of the constituent bonds in the PVC repeating unit. Hibi et al.<sup>30</sup> arrived at a value of  $10.4 \times 10^{-3}$  for the intrinsic birefringence. More recently, Robinson and Bower<sup>31</sup> reported a value of 13.0  $\times 10^{-3}$ , which they deduced from a study utilizing Raman spectroscopy. Based on the latter value, the maximum draw ratio of 4.2 at 100°C attained in this study corresponds to an orientation function of about 0.5.

In Figures 26 and 27, birefringence is again used to correlate the apparent solubility and diffusion coefficients of Ar and N<sub>2</sub> for samples drawn at 100°C. It was not possible to obtain  $D_a$  values for He because the time lags were immeasurably small for this gas. Figure 26 demonstrates how  $k_a$  is slightly



Fig. 26. Apparent solubility for Ar and  $N_2$  in PVC at 35°C vs. film birefringence. (Drawing temperature = 100°C.)



Fig. 27. Apparent diffusion coefficients for Ar and  $N_2$  in PVC at 35°C as a function of film birefringence.

decreased for both Ar and  $N_2$  by orientation. The effect of orientation on the solubility, however, was also dependent on the drawing temperature. This will be dealt with later where the effects of drawing temperature on gas transport are considered.

The response of  $D_a$  to orientation is more interesting as seen in Figure 27, where plots for Ar and N<sub>2</sub> against birefringence are shown. For both gases,  $D_a$  decreases with  $\Delta$  and the slopes of the curves become more negative as  $\Delta$  increases.

Annealing the polymer under strain subsequent to drawing, which causes a slight increase in density as seen in Figure 15, did not produce any significant further reductions in the transport parameters of the oriented film. A sample drawn 3.5X at 100°C and then annealed at this temperature for 15 more minutes had only 5% lower P and  $D_a$  values compared to the film not exposed to such post-drawing treatment. By comparing the density and DSC data of oriented specimens with those of the annealed ones, it becomes evident that the transport response to orientation is not related to the same processes governing the annealing behavior analyzed above. Thus, an alternative approach must be considered to explain the observed trends.

Free volume changes cannot be of use for explaining these responses since the density remains essentially constant during drawing, so that the process of gas transport will be considered from the activated state approach in which the diffusion coefficient D, in this case  $D_a$ , is given by the wellknown Arrhenius expression

$$D = D_0 e^{-E_D/RT} \tag{5}$$

where  $E_D$ , the activation energy, is known to be related to the cohesive energy density of the polymer<sup>42</sup> while the preexponential factor  $D_0$  can be related through Eyring's transition state theory to the activation entropy, which is, in turn, related to the entropic state of the polymer.

Deformation of a rubberlike network, as in the case of drawing above  $T_g$ , causes a reduction in the entropy of the network which according to the rubber elasticity theory is proportional to the quantity  $\Gamma$  defined as

$$\Gamma = [\lambda_1^2 + \lambda_2^2 + \lambda_3^2 - 3]$$
(6)

where the  $\lambda_i$  are deformation ratios along the three principal axes of the specimen. For uniaxial drawing at constant volume,

$$\lambda_2 = \lambda_3 = \frac{1}{\sqrt{\lambda_1}} = \frac{1}{\sqrt{\lambda}} \tag{7}$$

so that

$$\Gamma = [\lambda^2 + 2/\lambda - 3] \tag{8}$$

If one assumes that this change in entropy of the polymer on drawing translates into a change in the entropy of activation for diffusion, then  $\ln D_0$  should be linearly related to  $\Gamma$ . If this physical process of orientation does not change the activation energy  $E_D$ , then also  $\ln D$  should be linearly related to  $\Gamma$  since

$$\ln D = \ln D_0 - E_D / RT \tag{9}$$

Figure 28 shows plots of  $\ln D$  vs.  $\Gamma$  for Ar and N<sub>2</sub>. Interestingly, both sets of data form quite good straight lines (correlation coefficients for Ar and N<sub>2</sub> are -0.996 and -0.957, respectively) with essentially identical slopes.



Fig. 28. Apparent diffusion coefficients correlated with the rubber elasticity parameter.



Fig. 29. Apparent diffusion coefficient of Ar for heat-treated ( $\lambda = 1.0$ ) and drawn ( $\lambda = 4.2$ ) PVC plotted in the Arrhenius form.

To further examine the relative effect of drawing on the parameters  $D_0$ and  $E_D$ , the transport of Ar was measured as a function of temperature between the limits of 35 and 65°C. After the series of runs between 35 and 65°C, no measurable loss in birefringence for oriented samples was observed. Figure 29 shows an Arrhenius plot for apparent diffusion coefficients of Ar in PVC for samples with  $\lambda = 1.0$  and 4.2 prepared at 100°C. Drawing causes a very slight reduction in  $E_D$ , but the main effect is a reduction in the preexponential factor, consistent with the arguments outlined above and the results shown in Figure 28. These results differ from the findings of Barker et al.,<sup>6</sup> who report increases in  $D_0$  for poly(alkyl methacrylates). Ito,<sup>32</sup> on the other hand, obtained results similar to ours for CO<sub>2</sub> and polycarbonate.

Figures 30 and 31 present the permeability and apparent solubility coefficients from this series of transient permeation measurements using the Arrhenius form. Orientation causes an increase in both the activation energy  $E_P$  and the preexponential factor  $P_0$  for permeation. The net effect is that orientation has a larger effect on the permeability coefficient at low temperatures than at high temperatures. The effect of orientation on the apparent solubility coefficient is even more interesting in that the lines for the drawn and undrawn PVC cross such that the undrawn material has a greater temperature dependence, indicative of a larger apparent heat of solution. However, since  $k_a$  is a composite parameter equivalent to  $k_D + C'_H b$  in terms of the dual sorption model, the exact meaning of this trend is difficult to interpret without resolving this parameter into its individual



Fig. 30. Ar permeability for heat-treated ( $\lambda = 1.0$ ) and drawn ( $\lambda = 4.2$ ) PVC plotted in the Arrhenius form.



Fig. 31. Apparent solubility of Ar for heat-treated ( $\lambda = 1.0$ ) and drawn ( $\lambda = 4.2$ ) PVC plotted in the Arrhenius form.

components from detailed analysis of sorption isotherms, which was not done. The parameters deduced from the plots shown in Figures 29–31 for describing the temperature dependence of  $D_a$ ,  $k_a$ , and P are listed in Table V.

Wang and Porter<sup>7</sup> successfully correlated their data on drawn polystyrene using the Cohen and Turnbull free volume model, which can be written as

$$D = A \exp\left[\frac{-\gamma v^*}{\alpha v_m (T - T_0)}\right] \tag{10}$$

where A = empirical preexponential factor,  $v^* =$  critical volume required for a penetrant molecule to diffuse,  $v_m =$  actual volume of penetrant molecule,  $\gamma =$  an overlap factor (often close to unity), and  $\alpha =$  the planar thermal expansivity for the polymer. The anisotropy induced by drawing the polymer results in different linear expansivities along and perpendicular to the draw direction,  $\alpha_{\parallel}$  and  $\alpha_{\perp}$ , whose sum is equal to  $\alpha$ , so that eq. (10) can be rewritten as

$$D = A \exp\left[\frac{-\gamma v^*}{(\alpha_{\parallel} + \alpha_{\perp})v_m(T - T_0)}\right]$$
(11)

Since orientation has been found to reduce the quantity  $(\alpha_{\parallel} + \alpha_{\perp})$  relative to its value for the isotropic material, this change is expected to manifest itself as a reduction in *D*. A plot of ln *D* against  $(\alpha_{\parallel} + \alpha_{\perp})^{-1}$  should thus be also expected to yield a straight line as reported by Wang and Porter. Using

TABLE VActivation Energies, Preexponential Factors, and Heats of Solution for Ar Transport in<br/>Heat-Treated ( $\lambda = 1.0$ ) and Drawn ( $\lambda = 4.2$ ) PVC

Parameter	Heat-treated at 100°C $(\lambda = 1.0)$	Drawn at 100°C $(\lambda = 4.2)$	
$\overline{E_n (\text{kcal/mol})}$	8.879	10.35	
$P_0$ [cm <sup>3</sup> (STP)cm/cm <sup>2</sup> s cm Hg]	$5.576 imes10^{-6}$	$3.982 imes10^{-5}$	
$E_{Da}$ (kcal/mol)	12.917	12.40	
$D_{a0}$ (cm <sup>2</sup> /s)	3.998	1.266	
$\Delta H_s$ (kcal/mol)	-4.028	-2.056	
$k_{a0}$ [cm <sup>3</sup> (STP)/cm <sup>3</sup> atm]	$1.075 imes10^{-4}$	$2.379 imes10^{-3}$	

Hellwege's thermal expansivity data for uniaxially oriented PVC,<sup>43</sup> the above procedure was attempted by plotting ln  $D_a$  and ln P against ( $a_{\parallel}$  +  $\alpha_1$ )<sup>-1</sup>. Neither plot, however, yielded the expected linear dependence and both exhibited a strong curvature similar to that of Figure 27. PVC most probably differs from amorphous polystyrene in its degree of internal molecular order. One indication of this is the birefringence response to orientation above  $T_g$  in the two polymers. Polystyrene obeys the affine deformation mechanism, illustrated in Figure 32, which is characteristic of rubbers,<sup>7,29</sup> whereas PVC, like polycarbonate,<sup>44</sup> is found to allow a pseudoaffine deformation mechanism, which describes crystallite orientation in many semicrystalline polymers. Another difference is manifested in the dependence of the birefringence on the drawing temperature. As seen in Figure 12, PVC exhibits only about 20% reduction in  $\Delta$  by drawing at  $(T_g$ + 25) relative to the value for drawing at  $T_g$ . Over a similar temperature interval Wang and Porter<sup>45</sup> observed over a tenfold reduction in  $\Delta$  for atactic polystyrene.

#### **Effects of Processing Temperature**

The effects of drawing or heat-treatment on gas transport properties depend not only on the extent of orientation but also on the processing temperature employed. To study this temperature dependence, the parameters P,  $D_a$ , and  $k_a$  for Ar were measured for samples processed at temperatures ranging from 50 to 125°C at draw ratios of 1.0 and 3.0. The sample drawn at 50°C has a draw ratio of 2.8, which was the maximum attainable draw ratio at that temperature. Some data for N<sub>2</sub> followed similar trends to those reported here for Ar. We shall consider the effects of processing temperature on P,  $D_a$ , and  $k_a$  separately.

The behavior of  $D_a$  over the range of processing temperatures (50–125°C) is depicted in Figure 33. The curve for  $\lambda = 1.0$  exhibits a minimum in  $D_a$  at about 100–110°C. It is interesting that the location of this minimum almost coincides with that of the maximum for the endotherm area shown in Figure 20. In fact, the two trends are essentially mirror images of one another. Thus, the  $D_a$  data for annealed PVC correlate better with DSC endotherm data than they do with density. This response of  $D_a$  to annealing agrees well with Brady's findings for oxygen.<sup>5</sup> For samples drawn above  $T_g$  ( $\lambda = 3.0$ ),  $D_a$  follows a similar trend as for the undrawn material. However,



Fig. 32. Birefringence response to uniaxial drawing in two theoretical schemes of deformation. (Figure adapted from Ref. 29.)

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Fig. 33. Apparent diffusion coefficient of Ar in PVC at 35°C vs. processing temperature for annealed ( $\lambda = 1.0$ ) and drawn ( $\lambda = 3.0$ ) samples.

at high drawing temperatures, the 3X curve is expected to increase more rapidly since the birefringence declines with increasing temperature as shown in Figure 12.

The behavior of  $D_a$  for the two samples processed below  $T_g$  is quite unexpected. As the treatment temperature is lowered from  $T_g$ ,  $D_a$  increases, reaches a maximum, and then returns to the base value for the as-received film at temperatures below 50°C. The increase in  $D_a$  seems consistent with the density data for sub- $T_g$ -annealing shown in Figure 14. However, Illers,<sup>35</sup> for example, reported significant decreases (~30%) in P as a result of annealing just below  $T_g$ . The DSC scans of Figure 21 show no features for the 70°C-annealed sample other than the well-known shift in position and height of the sub- $T_g$  relaxation peak. For the sub- $T_g$  drawn samples,  $D_a$  is about 15% lower than for the "as-received" material. It must be noted that the annealing time for the sample annealed at 55°C was 36 h instead of the 15 min used uniformly for all other samples. This exception was made considering the slow relaxation rate for the polymer 20°C below its  $T_g$ .

The apparent Ar solubility data for annealed and drawn PVC are reported in Figure 34. The effects of processing temperature on  $k_a$  result in bell-



Fig. 34. Apparent solubility of Ar in PVC at 35°C vs. processing temperature for annealed ( $\lambda = 1.0$ ) and drawn ( $\lambda = 3.0$ ) samples.

shaped curves that have their maxima at 100 and 90°C, for the 1X and 3X samples, respectively. A very similar curve for the  $k_a$  of  $O_2$  ws reported by Brady et al.<sup>5</sup> in the case of the annealed samples, but the results for drawn materials cannot be compared since Brady's work was limited to biaxial orientation. The 3X data exhibit a more narrow and pronounced maximum than for the annealed samples.

The maxima in Figure 34 correspond approximately to the minima in  $D_{a}$ seen in Figure 33. The sorption maxima are apparently another manifestation of the temperature dependent "ordering" process indicated by the DSC results shown in Figure 20. As explained earlier, annealing at temperatures above  $T_{e}$  alters the microstructural organization on the molecular or segmental level. The rate of this process is highest at temperatures that are moderately above  $T_g$ . At  $T_g$ , segmental motions are still somewhat restricted while at temperatures 50°C above  $T_g$  vigorous backbone mobility tends to destroy any induced molecular order-a situation somewhat analogous to the interplay of kinetic and thermodynamic factors in crystallization. Since  $(T_g + 50^{\circ}\text{C})$  generally defines the onset of liquidlike backbone mobility in polymers, an annealing temperature of  $(T_g + 25^{\circ}C)$  or 100°C seems reasonable for inducing the highest level of order in PVC. This temperature shifted to 90°C for the oriented samples, presumably because in the oriented state only shorter polymer segments are free to participate in cooperative motions, leading to ordered structures since longer segments are restrained by the segments elongated under strain.

The reasons that the apparent solubility is highest at processing temperatures near 90-100°C appear to stem from the decreased mobility of segments associated with the structural order, which results in greater propensity for intersegmental void regions to serve as gas sorption sites. The gradual loss of this molecular order at processing temperatures above 90-100°C is also evident in Figure 33 from the trend towards increased  $D_a$ at higher processing temperatures.

Finally, the effects of processing temperature on the permeability of annealed and drawn PVC to Ar and He are shown in Figure 35. The permeability data reflect the combined effects of mobility and solubility discussed separately above. For annealed samples the permeability decreases essen-



Fig. 35. PVC permeability to He and Ar at 35°C vs. processing temperature for annealed ( $\lambda = 1.0$ ) and drawn ( $\lambda = 3.0$ ) samples.

tially monotonically, leveling off above about 90°C. Annealing at temperatures above 125°C increases the permeability again according to Brady's study, but such high temperatures were not investigated in this work. For samples drawn at temperatures 90°C or below, the permeabilities are essentially constant. Between 90 and 100°C, P for Ar drops abruptly by 17% owing to the reduction in solubility observed in Figure 34. Beyond 100°C, P increases slightly with higher drawing temperatures. The same trends but to a lesser extent were observed for He.

## CONCLUSIONS

Several conclusions can be drawn from the findings of this investigation. The sorption of  $CO_2$  in PVC is much higher than expected on the basis of established correlations and comparisons with other polymers. This is believed to stem from a specific interaction between  $CO_2$  and the PVC repeating unit which increases the amount of  $CO_2$  dissolved by the Henry's law mode since the amount sorbed by the Langmuir mode appears normal. This interaction-specific sorption is believed to be responsible for the extreme plasticizing or conditioning effects observed for  $CO_2$  and PVC. Annealing PVC at temperatures above  $T_g$  induces some form of molecular order in the polymer. This order is accompanied by a rise in density and the appearance of endothermic peaks in the DSC thermograms. The highest level of order is achieved by annealing at temperatures around  $(T_g + 25^{\circ}C)$ . A minimum in the apparent diffusion coefficient for Ar was observed for this region of annealing temperatures.

Uniaxial drawing has some effect on gas solubility in the polymer, but this depends on the drawing temperature. The effect is most pronounced at drawing temperatures  $\sim (T_g + 25^{\circ}\text{C})$ . The apparent diffusion and solubility coefficients are dependent on the drawing temperature employed but in different ways. For example,  $D_a$  undergoes a *minimum* at processing temperatures of 90–100°C depending on the draw ratio, whereas  $k_a$  goes through a *maximum* in the same temperature region.

The permeability and diffusion coefficients decrease with increasing extent of uniaxial molecular orientation in PVC. These reductions are the result of an increased permeation activation energy  $E_p$  and a reduced diffusion preexponential factor  $D_0$ . The diffusion activation energy  $E_D$  remained essentially constant with orientation, but the increase in  $E_p$  was brought about by a reduced apparent heat of solution with orientation. Due to these factors, the effectiveness of molecular orientation in improving the barrier character of PVC is best at low temperatures. Finally, while both annealing above  $T_g$  and molecular orientation reduce the permeation and diffusion of gases in PVC, they appear to do so via different mechanisms.

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